

Students will recognize, analyze and graph the equations of the conic sections.

I. For each parabola, write the equation in standard form, state the vertex, the focus and the directrix and then graph.

1. $x^2 - 8y = 0$ $x^2 = 8y$ $v: (0, 0)$ $f: (0, 2)$ $dir: y = -2$
 $4p = 8$
 $p = 2$

2. $(x - 2)^2 = 8(y + 1)$ $v: (2, -1)$ $f: (2, 1)$ $dir: y = -3$
 $4p = 8$
 $p = 2$

3. $(y + 2)^2 = -16(x - 3)$ $v: (3, -2)$ $f: (-1, -2)$ $dir: x = 7$
 $-16 = 4p$
 $p = -4$

4. $(x + 1)^2 + 8(y + 2) = 0$ $v: (-1, -2)$ $f: (-1, -4)$ $dir: y = 0$
 $(x + 1)^2 = -8(y + 2)$
 $4p = -8$ $p = -2$

5. $(x + 3) + (y - 2)^2 = 0$ $v: (-3, 2)$ $f: (-3\frac{1}{4}, 2)$ $dir: x = -2\frac{3}{4}$
 $(y - 2)^2 = -(x + 3)$
 $4p = -1$ $p = -\frac{1}{4}$

6. ~~$x^2 - 2x - 12y + 13 = 0$~~ $v: (-4, 2)$ $f: (-4, 1)$ $dir: y = 3$
 $x^2 + 8x = -4y - 8$
 $(x + 4)^2 = -4(y - 2)$


7. $-4x + 4 = y^2 + 10y + 25$ $v: (1, -5)$ $f: (0, -5)$ $dir: x = 2$
 $(y + 5)^2 = -4(x - 1)$
 $p = -1$

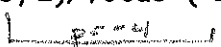
8. $x^2 - 2x - 12y + 13 = 0$ $v: (1, 1)$ $f: (1, 4)$ $dir: y = -2$
 $x^2 - 2x = 12y - 13$
 $(x - 1)^2 = 12(y - 1)$


9. $4x^2 - 40y - 24x - 4 = 0$ $v: (3, -1)$ $f: (3, 1\frac{1}{2})$ $dir: y = -3\frac{1}{2}$
 $x^2 - 6x + 9 = 10y + 10$ $4p = 10$
 $(x - 3)^2 = 10(y + 1)$ $p = \frac{5}{2}$

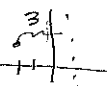
10. $2x^2 - 16x + 16y + 64 = 0$ $v: (4, -2)$ $f: (4, -4)$ $dir: y = 0$
 $x^2 - 8x = -8y - 32 + 16$
 $(x - 4)^2 = -8(y + 2)$
 $4p = -8$
 $p = -2$


II. Given the following information, write the standard form for each parabola.

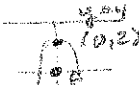
11. Vertex: (3, 2); focus: (1, 2) $(y-2)^2 = -8(x-3)$



12. Vertex: (3, 2); focus: (-1, 2) $(y-2)^2 = -16(x-3)$



13. Vertex: (0, 4); directrix: $y = 2$ $x^2 = 8(y-4)$


14. Vertex: (-2, 1); directrix: $x = 1$ $(y-1)^2 = -12(x+2)$


15. Focus: (2, 2); directrix: $x = -2$ $(y-2)^2 = 8x$


16. Focus: (0, 0); directrix: $y = 4$ $(x)^2 = -8(y-2)$


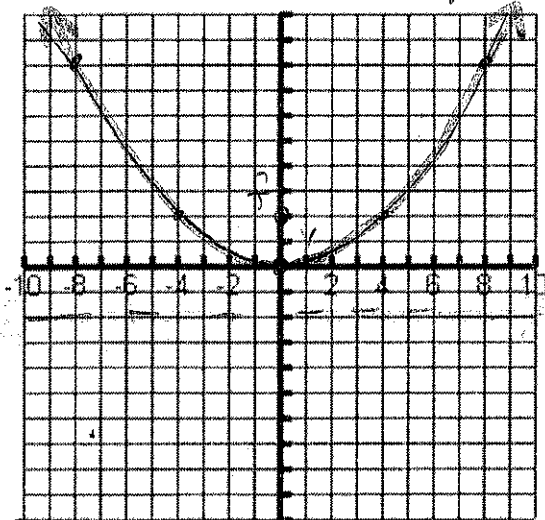
17. Vertex: (0, 0); focus: (0, -2) $x^2 = -8y$


18. Vertex: (0, 0); directrix: $x = 3$ $y^2 = -12x$


19. Focus: (2, 5); directrix: $x = 3$ $(y-5)^2 = -2(x-2\frac{1}{2})$

20. Focus: (1, 3); vertex: (1, 2) $(x-1)^2 = 4(y-2)$

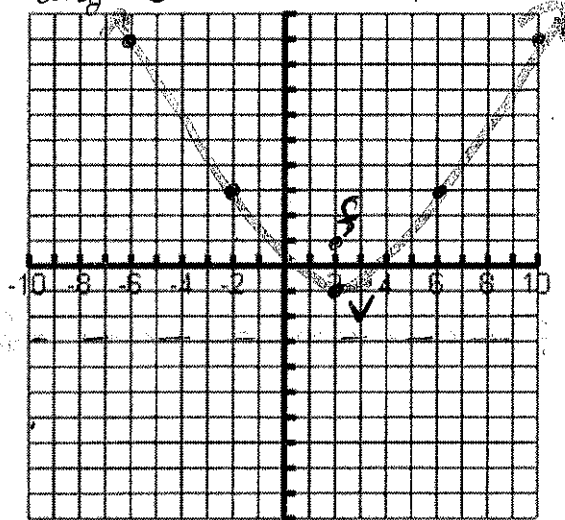
① $x^2 = 8y$ vertex: (0,0)
 $4p = 8$ focus: (0,2)
 $p = 2$ dir: $y = -2$



② $(x-2)^2 = 8(y+1)$ vertex: (2,-1)
 $p = 2$ focus: (2,1)
dir: $y = -3$

10	9
-6	9
6	3

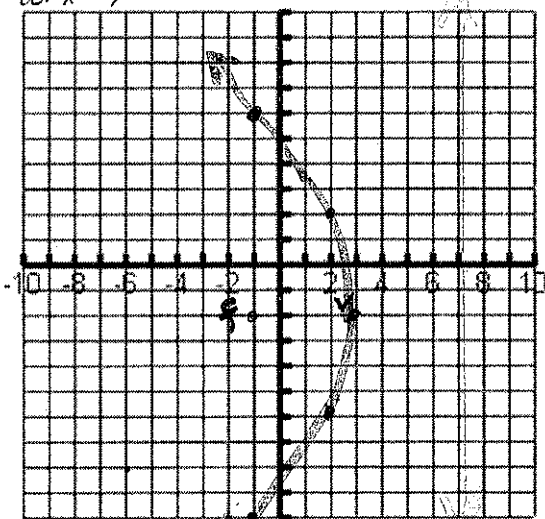
 $y = \frac{(x-2)^2}{8} + 1$



③ $(y+2)^2 = -16(x-3)$ vertex: (3,-2)
focus: (-1,-2)
dir: $x = 7$

-1	6
2	2

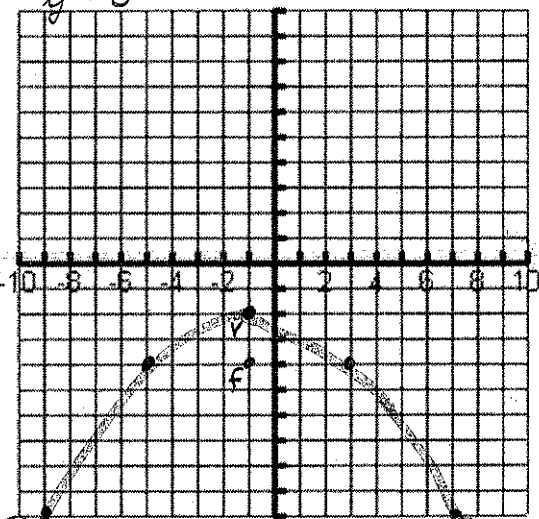
 $x = \frac{(y+2)^2}{-16} + 3$



④ $(x+1)^2 + 8(y+2) = 0$ vertex: (-1,-2)
focus: (-1,-4)
dir: $y = 0$

7	-10
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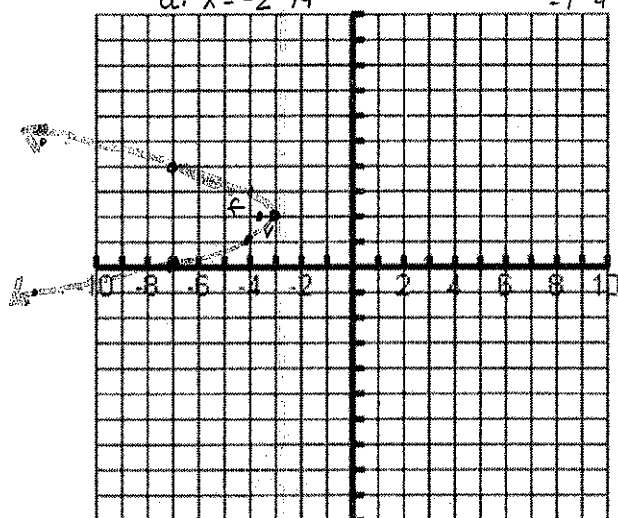
 $y = \frac{(x+1)^2}{-8} - 2$



⑤ $(y-2)^2 = -(x+3)$ vertex: (-3,2)
focus: (-3 1/4, 2)
dir: $x = -2 3/4$

-4	3
-4	1
-7	10
-7	4

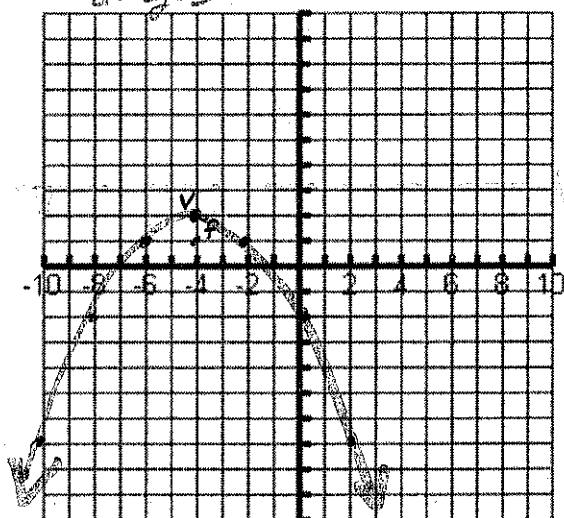
 $x = \frac{(y-2)^2}{-1} - 3$



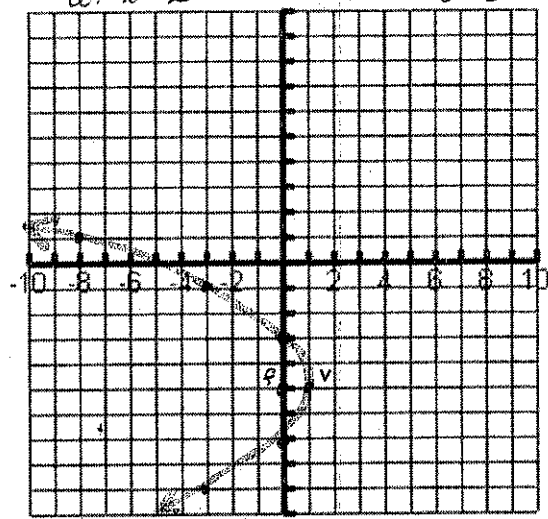
⑥ $(x+4)^2 = -4(y-2)$ vertex: (-4,2)
focus: (-4,1)
dir: $y = 3$

7	-10
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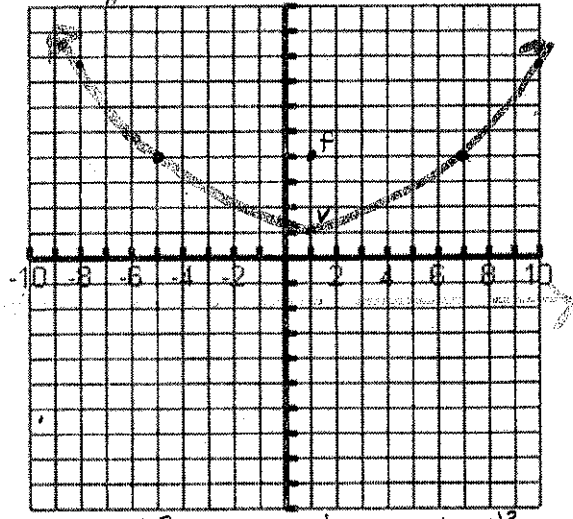
 $y = \frac{(x+4)^2}{-4} + 2$



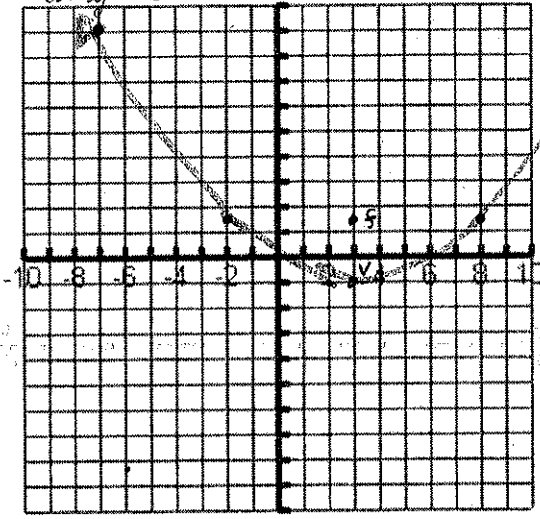
⑦ $(y+5)^2 = -4(x-1)$ $x = \frac{(y+5)^2}{-4} + 1$
 V: (1, -5)
 F: (0, -5)
 d: $x = 2$



⑧ $(x-1)^2 = 12(y-1)$ $y = \frac{(x-1)^2}{12} + 1$
 V: (1, 1)
 F: (1, 4)
 d: $y = -2$



⑨ $(x-3)^2 = 10(y+1)$ $y = \frac{(x-3)^2}{10} - 1$
 V: (3, -1)
 F: (3, 1/2)
 d: $y = -3 1/2$



⑩ $(x-4)^2 = -8(y+2)$ $y = \frac{(x-4)^2}{-8} - 2$
 V: (4, -2)
 F: (4, -4)
 d: $y = 0$

