

60. $\cos 2x = (-1)$ Evaluate

$$2x = \pi$$

$$x = \frac{\pi}{2}$$

$$x = \frac{\pi}{2} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

61. $\sin 2x + \sin x = 0$

$$2 \sin x \cos x + \sin x = 0$$

$$\sin x (2 \cos x + 1) = 0$$

$$\sin x = 0 \quad 2 \cos x + 1 = 0$$

$$x = 0, \pi$$

$$\cos x = -\frac{1}{2}$$

$$x = \pi n \text{ where } n \in \mathbb{Z}$$

$$x = \frac{2\pi}{3} + 2\pi n$$

$$x = \frac{4\pi}{3} + 2\pi n$$

62. $\cos 2x - \cos x = 0$

$$2 \cos^2 x - 1 - \cos x = 0$$

$$2 \cos^2 x - \cos x - 1 = 0$$

$$2x^2 - x - 1 = 0$$

$$m: -2$$

$$A: -1$$

$$(-2, 1)$$

$$2x^2 - 2x + x - 1 = 0$$

$$2x(x-1) + 1(x-1) = 0$$

$$(2x+1)(x-1) = 0$$

$$(2 \cos x + 1)(\cos x - 1) = 0$$

$$2 \cos x + 1 = 0$$

$$\cos x = -\frac{1}{2}$$

$$x = \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$\cos x - 1 = 0$$

$$\cos x = 1$$

$$x = 0$$

$$x = \frac{2\pi}{3} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

$$x = \frac{4\pi}{3} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

$$x = 2\pi n$$

$$63. \cos \frac{x}{2} - \sin x = 0$$

$$\left(+ \sqrt{\frac{1 + \cos A}{2}} \right)^2 = \left(+ \sin x \right)^2$$

$$\frac{1 + \cos A}{2} = \sin^2 x$$

$$\frac{1 + \cos A}{2} = 1 - \cos^2 x$$

$$\frac{1}{2} + \frac{1}{2} \cos A = 1 - \cos^2 x$$

$$-1 + \cos^2 x \quad -1 + \cos^2 x$$

$$\cos^2 x + \frac{1}{2} \cos A - \frac{1}{2} = 0$$

$$2 \cos^2 x + \cos A - 1 = 0$$

$$M = -2$$

$$A = 1$$

$$(2r-1)$$

$$\boxed{2 \cos^2 x + \cos x - 1} = 0$$

$$2 \cos x (\cos x + 1) - 1 (\cos x + 1) = 0$$

$$2 \cos x - 1 = 0$$

$$\cos x = \frac{1}{2}$$

$$x = \frac{\pi}{3}, \frac{5\pi}{3}$$

$$\cos x + 1 = 0$$

$$\cos x = -1$$

$$x = \pi$$

$$x = \frac{\pi}{3} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

$$x = \frac{5\pi}{3} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

$$x = \pi + 2\pi n, \text{ where } n \in \mathbb{Z}$$

64. $\sqrt{\frac{1-\cos A}{2}} + \cos x = 0$

$$\left(\sqrt{\frac{1-\cos A}{2}}\right)^2 = (-\cos x)^2$$

$$\frac{1-\cos A}{2} = \cos^2 x$$

$$0 = \cos^2 x + \frac{\cos x}{2} - \frac{1}{2}$$

$$0 = 2\cos^2 x + \cos x - 1$$

M: -2

A: 1

$$0 = 2\cos^2 x + 2\cos x - \cos x - 1$$

See problem 63 For rest of work

65. 

$$\cos 2x = 3\sin x + 2$$

$$1 - 2\sin^2 x = 3\sin x + 2$$

$$0 = 2\sin^2 x + 3\sin x + 1$$

M: 2

A: 3

$$0 = 2\sin^2 x + 2\sin x + \sin x + 1$$

$$0 = 2\sin x (\sin x + 1) + 1(\sin x + 1)$$

$$2\sin x + 1 = 0$$

$$\sin x = -\frac{1}{2}$$

$$x = \frac{11\pi}{6}, \frac{7\pi}{6}$$

$$\sin x + 1 = 0$$

$$\sin x = -1$$

$$x = \frac{3\pi}{2}$$

$$x = \frac{11\pi}{6} + 2\pi n, \text{ where } n \in \mathbb{Z}$$

$$x = \frac{7\pi}{6} + 2\pi n$$

$$x = \frac{3\pi}{2} + 2\pi n$$