

I. Evaluate. (Exact values)

1.  $\arcsin\left(\frac{1}{2}\right)$

2.  $\arctan\left(\frac{\sqrt{3}}{3}\right)$

3.  $\arccos\left(-\frac{\sqrt{2}}{2}\right)$

II. Identify the amplitude, period, midline, and phase shift.

4.  $y = \cos(x - \pi)$

5.  $y = -5\cos\left(\frac{x}{4} - \pi\right) + 4$

6.  $y = \frac{1}{2}\sin\left(2x - \frac{\pi}{3}\right)$

7.  $y = -3 + \sin\left(3x + \frac{\pi}{2}\right)$

III. Graph the functions below. Identify the transformations.

8.  $y = \cos\left(2x - \frac{\pi}{2}\right)$

9.  $y = 3\sin(3x + \pi) - 5$

10.  $y = -\sin\left(2x - \frac{\pi}{3}\right)$

11.  $y = -2\cos(3x) + 4$

IV. Identify the domain, range, period, and asymptotes of each graph.

12.  $y = \cot\left(x + \frac{\pi}{2}\right)$

13.  $y = -2\csc(4x)$

14.  $y = \sec 4x$

15.  $y = 4\cot(3x)$

16.  $y = \cot\left(\frac{x}{4}\right)$

V. Sketch the parent graphs of sine and cosine.  
17. – 18.

VI. Write the equation of a cosine function with the following conditions.

19. amplitude = 2, period =  $\frac{\pi}{2}$ , phase shift =  $-\frac{\pi}{4}$

20. period =  $2\pi$ , phase shift = -1, vertical shift = -4

VII. Find two angles,  $\theta$ , between  $[0^\circ, 360^\circ)$  that satisfy the given equation.

21.  $\cot\theta = -1.456$

22.  $\sin\theta = .9564$

23.  $\tan\theta = 0.3519$

24.  $\sec\theta = -2.6571$

VIII. Solve the word problems below.

25. A man that is 6 feet tall casts a shadow 14 feet long. Find the angle of elevation of the sun.

26. From a point on a cliff 75 feet above water level an observer can see a ship. Find the angle of depression to the ship if the ship is 400 feet from the base of the cliff.

27. A ladder is leaning against a wall. The base of the ladder is 5 feet from the wall and makes an angle of  $39^\circ$  with the ground. Find the length of the ladder.

28. Find the altitude of a scalene triangle if one of the base angles measures  $70^\circ$  and its adjacent side (not the base) is 9 cm.

29. The bearing of a buoy from a ship 8.7 miles away is  $N64^\circ E$ . The ship is headed due north, and the navigator plans to change course when the buoy has a bearing of  $S26^\circ E$ . How much farther will the ship travel before a change of course is required?

30. The navigator of a ship on a  $N44^\circ E$  sights a buoy with a bearing of  $S46^\circ E$ . After the ship sails 15 km along the same course, the navigator sights the same buoy with a bearing  $S12^\circ E$ . Find the distance between the ship and the buoy at the time of each sighting.

IX. Evaluate.

31.  $\arcsin(\sin 3\pi)$

32.  $\cos\left(\arccos\left(-\frac{\sqrt{3}}{2}\right)\right)$

33.  $\arctan\left(\tan\left(\frac{11\pi}{6}\right)\right)$